## Unit 3 Radical and Rational Functions <br> Study Guide

This test will be out of 64 points.
What is the make-up of the test?

- 7 Multiple Choice
- 19 Free Response

You will have the whole class period to complete this test. Come with specific questions if you have them before the test as there will be no review.

What should I expect to see?

- Inverse and Direct variation
- Solving Radical Equations
- Solving Rational Equations
- Transformations from Parent Function
- Graphing Radical Functions
- Graphing Rational Functions
- Identifying Key Features in Graphs
- Moving between Radical and Exponential Form


## Steps for Solving Equations:


**Extraneous Solutions are answers that are algebraically correct, but do not serve as solutions.**

## Graphing Equations:

Radical:
**Horizontal Translation outside of radical.
(+) Up ( - ) Down
**Vertical Translation is inside with x .
(+) Left ( - ) Right
**Reflections over axes as seen by negative Outside Radical (x) Inside Radical (y)
**Dilations: $a>1$ Stretch $a<1$ Shrink

When graphing we start by finding the vertex
Vertex - opposite value under radical for x , same value outside radical for $y$.

Next we follow a similar pattern to quadratic if no dilation has occurred.

From the vertex over 1, up 1. Back to the vertex over 4, up 2. Back to the vertex over 9, up 3.

If dilation has occurred, you will need to adjust your "over" value by multiplying with scale factor.

Rational: (Letters correspond to those in foldable!)
**Horizontal Translation outside fraction, k value.
(+) Up
(-) Down

Horizontal Asymptote: $\mathrm{y}=\mathrm{k}$ (value outside fraction.)

The range is all real numbers except $\mathrm{y} \neq \mathrm{k}$
**Vertical Translation in denominator with x .
(+) Left
(- ) Right

Vertical Asymptote: $\mathrm{x}=\mathrm{h}$ (opposite value with x )
The domain is all real numbers except $\mathrm{x} \neq \mathrm{h}$

Dilations: $|\mathrm{a}|>1$ Stretch $|\mathrm{a}|<1$ Shrink

Reflections:
When a is positive function decreases and branches are in Quadrants I and III.

When a is negative function increases and branches are in Quadrants II and IV. (Reflection in x axis)

## Special Relationships:

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Direct Variation:
- When \(x\) increases, \(y\) increases
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- When $x$ decreases, $y$ decreases

Follows the form: $\mathrm{y}=\mathrm{kx}$
Solve for $k$ : $\quad k=y / x$

## Inverse Variation:

- When x increases, y decreases
- When $x$ decreases, $y$ increases

Follows the form: $y=k / x$
Solve for $k$ : $\quad k=y(x)$
${ }^{* *}$ There are also videos under homework to help with concepts that you are struggling on. ${ }^{* *}$

